

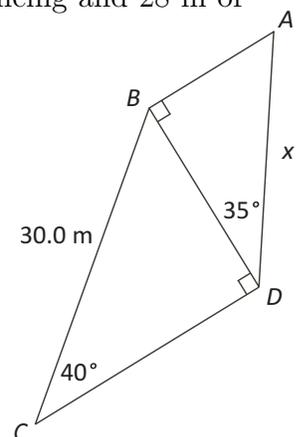


Mathematics Teachers Enrichment Program

MTEP 2012

Trigonometry and Bearings: Exercises

1. In $\triangle ABC$, $\hat{A}BC = 90^\circ$, $AB = 8$ and $BC = 15$. Solve $\triangle ABC$. Round side length and angles to one decimal, as necessary.
2. Solve $\triangle XYZ$, given $X\hat{Z}Y = 90^\circ$, $X\hat{Y}Z = 41^\circ$, and $XY = 20$. Round side lengths to one decimal, as necessary.
3. At a point 50 m from the base of a tower the angle of elevation to the top of the tower is 70° . Determine the height of the tower, to the nearest metre.
4. From the top of a 40 m tower, an observer measures the angle of depression to a boat in the water below to be 28° . How far, to the nearest metre, is the boat from the base of the tower?
5. A 12.4 m flagpole is placed on top of a tall building. An observer, standing directly in front of the building and flagpole, measures the angle of elevation to the bottom of the flagpole to be 42.5° and to the top of the flagpole to be 48.2° . Determine the height of the building, to the nearest metre.
6. To calculate the height of a tower, David measured the angle of elevation of the top of the tower from a point A to be 42° . He then moved 30 m closer to the tower and from point B measured the angle of elevation to the top of the tower to be 50° . To the nearest metre, determine the height of the tower.
7. Determine the length of BC in $\triangle ABC$ where $AB = 10$, $AC = 9$ and $B\hat{A}C = 58^\circ$. Round correctly to one decimal place.
8. Determine the size of the largest angle in $\triangle PQR$ where $PQ = 9$, $QR = 15$ and $PR = 11$. Round correctly to one decimal place.
9. In $\triangle XYZ$, $X\hat{Y}Z = 43^\circ$, $X\hat{Z}Y = 73^\circ$ and $YZ = 25$. Solve $\triangle XYZ$, rounding correctly to one decimal place.
10. In $\triangle DEF$, $DE = 9.4$, $EF = 17.5$ and $DF = 12.8$. Solve $\triangle DEF$. rounding each angle to one decimal place.
11. A triangular piece of land is bounded by 32 m of brick wall, 50 m of fencing and 28 m of road along the front. What angle does the fence make with the road?
12. Determine the length of x on the diagram to the right correct to one decimal place.
13. The bearing from A to B is 160° . What is the bearing from B to A ?





14. From an observation point in a fire tower, the observer spots a fire 5 km away at a bearing 130° . The observer also spots a village 2 km away on a bearing 240° . How far is the fire away from the village?
15. A hiker walks 1.5 km on a bearing 035° . At this point he turns directly south and walks 3.5 km. How far and on what bearing must he walk to return to his original starting point?
16. Two ships, R and Q , left a port, P , at the same time. After two hours, R had travelled 8 km on a bearing 075° from port and Q had travelled 10 km on a bearing 305° from port. How far apart are the two ships after two hours?
17. A tour boat leaves port and travels 15 km on a bearing of 088° and then travels a further 24 km on a bearing of 145° . The boat then returns directly to the starting point. Determine the distance to the port and the bearing along which the tour boat must travel.
18. Two towns, A and B , lie on longitude 37°W . Their latitudes are 50.4°N and 72.6°N , respectively. Calculate the shortest distance between the two towns.
19. Two towns, C and D , lie on the same longitude. Their latitudes are 80°N and 70°S , respectively. Calculate the shortest distance between the two towns.
20. Two cities, A and B , lie on the Equator, one at longitude 65°E and the other at longitude 23°W . Calculate the distance between the two towns, measured along the Equator.
21. Find the distance, measured along a meridian, from any point on parallel of latitude 30°N to the North Pole.
22. Two towns are located on longitude 50°E . The towns are 5 200 km apart. Calculate the difference in their latitudes.
23. Find the length of the parallel of latitude 41°S .
24. Two places are located on the parallel of latitude 32°N , one at longitude 47°W and the other at longitude 25°E .
 - a) How far apart are the two towns, measured along the parallel of latitude 32°N ?
 - b) If it takes a plane 10 hours to travel from one town to the other, calculate the speed of the plane, correct to the nearest kilometer per hour.
25. Two towns, P and Q , are located at $(4^\circ\text{N}, 100^\circ\text{E})$ and $(4^\circ\text{N}, 140^\circ\text{E})$, respectively. Calculate the shortest distance from P to Q , along the parallel of latitude 4°N .
26. Havana and Canton are both on latitude 23°N , and their longitudes are 82.25°W and 113.25°E , respectively. Find their distance apart measured along the parallel of latitude.
27. Cherepovets, Russia is located approximately at $(60^\circ\text{N}, 38^\circ\text{E})$ and Mt. Logan, Canada is located approximately at $(60^\circ\text{N}, 142^\circ\text{W})$.
 - a) How far apart are the two locations, measured along the parallel of latitude 60°N ?
 - b) Calculate the great circle distance between Cherepovets and Mt. Logan.